# 

BAHRIA UNIVERSITY KARACHI CAMPUS

**Department of Software Engineering**

**COURSE: GSL 321**

**NUMERICAL ANALYSIS**

**PROJECT Proposal**

**CLASS: BSE – 7B (FALL - 2023)**

**Analyzing and Implementing Iterative Linear System Solvers: Gauss-Jacobi, Gauss-Seidel, and Successive Over-Relaxation (SOR) Methods**

**Group Members**

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# **INTRODUCTION & BACKGROUND**

Linear systems, represented as (Ax = b), play a pivotal role in mathematical modeling across scientific and engineering domains. This project delves into the implementation and comparison of three iterative methods—Gauss-Jacobi, Gauss-Seidel, and Successive Over-Relaxation (SOR). These methods are essential for approximating solutions to large-scale linear systems encountered in applications such as structural analysis and fluid dynamics. The Gauss-Jacobi method, renowned for its simplicity, is augmented by the Gauss-Seidel method, which updates variables more dynamically. Successive Over-Relaxation (SOR) further refines convergence by introducing a relaxation parameter. This project aims to not only implement these methods but also analyze their convergence rates, stability, and computational efficiency, providing valuable insights for optimizing solutions to practical problems.

# **PROBLEM STATEMENT**

Effectively solving large linear systems is crucial in various fields, and iterative methods like Gauss-Jacobi, Gauss-Seidel, and Successive Over-Relaxation (SOR) offer solutions. However, understanding their behavior and choosing the right method for specific scenarios remains a challenge. This project aims to investigate the convergence, stability, and efficiency of these methods in different situations, addressing key questions such as their performance in diverse linear systems and the impact of parameters.

# **PROPOSED SOLUTION**

## 3.1. FEATURES OF THE PROJECT

The project will implement and assess the Gauss-Jacobi, Gauss-Seidel, and Successive Over-Relaxation (SOR) methods in Python, focusing on understanding their strengths and weaknesses. Key features include:

* **Method Implementation:** Code development in Python for the three iterative methods.
* **Convergence Analysis:** Systematic evaluation of convergence behavior under varying conditions to identify strengths and weaknesses.
* **Visualization:** Use of Matplotlib for clear visualization of convergence patterns and other relevant metrics.

## 3.2. METHODOLOGY

* **Implementation:** Code development in Python, ensuring simplicity and clarity in the implementation of the Gauss-Jacobi, Gauss-Seidel, and SOR methods.
* **Convergence Analysis:** Systematic testing and analysis of convergence rates for different types of linear systems.
* **Visualization:** Clear graphical representation of convergence behavior and other performance metrics using Matplotlib.

## 3.3. TECHNOLOGIES TO BE USED

* **Programming Language:** Python for its simplicity and readability.
* **Visualization:** Matplotlib for creating visualizations that aid in understanding the strengths and weaknesses of the implemented methods.

# **PROJECT SCOPE**

The scope of this project is defined by its focus on implementing and evaluating the Gauss-Jacobi, Gauss-Seidel, and Successive Over-Relaxation (SOR) methods for solving linear systems using Python. The project's boundaries and objectives include:

* **Implementation:** Develop Python code for the three iterative methods with a primary emphasis on simplicity, efficiency, and clarity.
* **Method Evaluation:** Conduct a comprehensive analysis of the implemented methods, assessing their strengths and weaknesses in terms of convergence rates, stability, and computational efficiency.
* **Parameter Sensitivity:** Investigate the impact of relaxation parameters, especially in the SOR method, on the convergence behavior to provide insights into optimal parameter selection.
* **Visualization:** Utilize Matplotlib for visual representation of convergence patterns and other relevant metrics, aiding in the interpretation of method performance.
* **Real-world Applications:** Apply the implemented methods to practical linear systems inspired by real-world scenarios in engineering and science to assess their applicability and performance.

# **PROJECT ABSTRACT**

This project involves implementing Gauss-Jacobi, Gauss-Seidel, and Successive Over-Relaxation methods in Python to solve linear systems. The focus is on evaluating their strengths and weaknesses in terms of convergence, stability, and efficiency. Utilizing Matplotlib for visualization, the project includes a parameter sensitivity study, emphasizing the impact of relaxation parameters in the SOR method. Real-world applications will be simulated to assess practical performance. The goal is to provide practical insights into optimizing the use of these iterative methods for solving large-scale linear systems.

# **MODULE DISTRIBUTION**

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| --- | --- | --- |
| **Name** | **Enrollment #** | **Module** |
| Muhammad Amjad | 02-131202-041 | SOR Method, Visualization |
| Jamshed Ali | 02-131202-008 | Guass Siedel Iteration Method |
| Abu Hurara | 02-131202-016 | Guass Jacobi Method |

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